

SIRGAS2018 GEOCENTRIC
REFERENCE SYSTEM FOR
THE AMERICAS

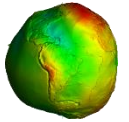
Aguascalientes, Mexico

Preliminary tests on BVRN new representation through Normal Heights based on GGMs and discrete GNSS observations

E. Nicacio & R. Dalazoana & S. R. C. De Freitas

Aguascalientes, Mexico – November 11th, 2018

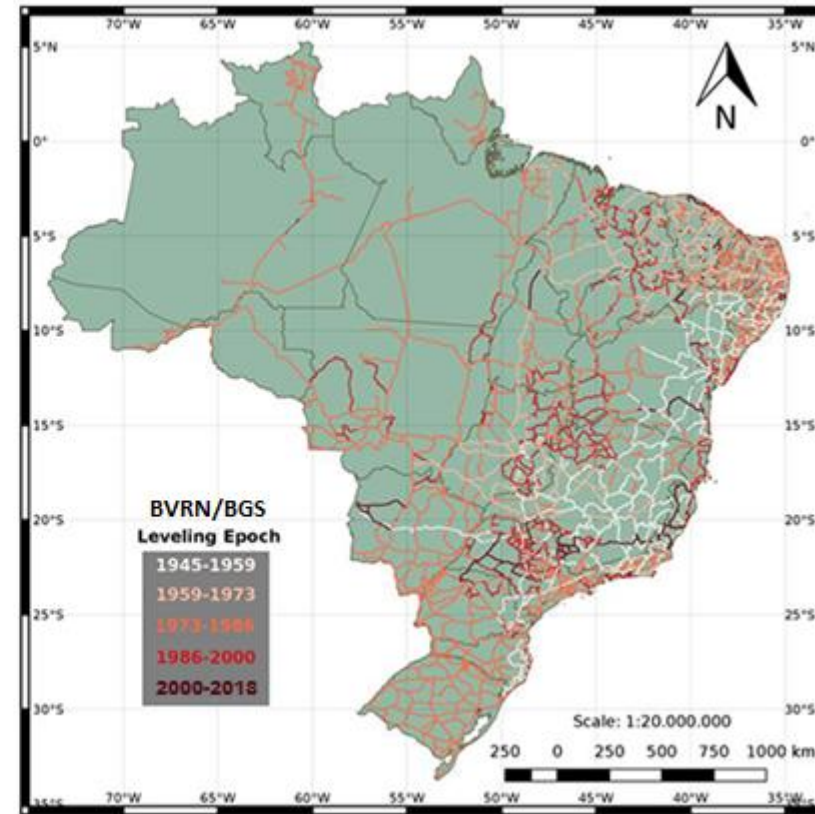
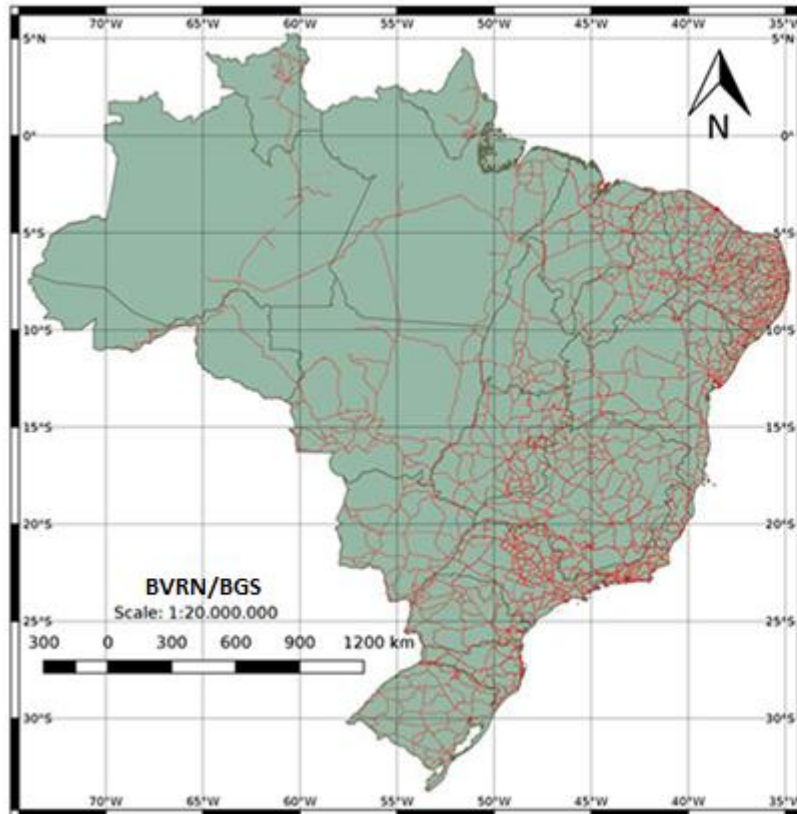
Introduction



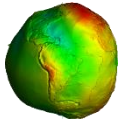
▶ Brazilian Vertical Reference Network (BVRN)

- ▶ One of the networks that integrate the Brazilian Geodetic System (BGS) and under responsibility of Brazilian Institute of Geography and Statistics (IBGE);

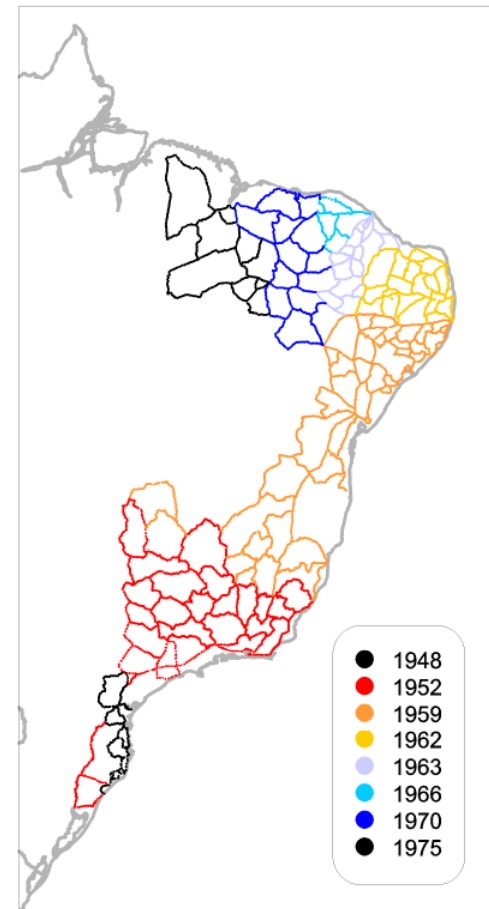
- Currently: ~ 70,000 benchmarks
- 2 reference tide gauges: DVB-I (Imbituba-SC) and DVB-S (Santana-AP);



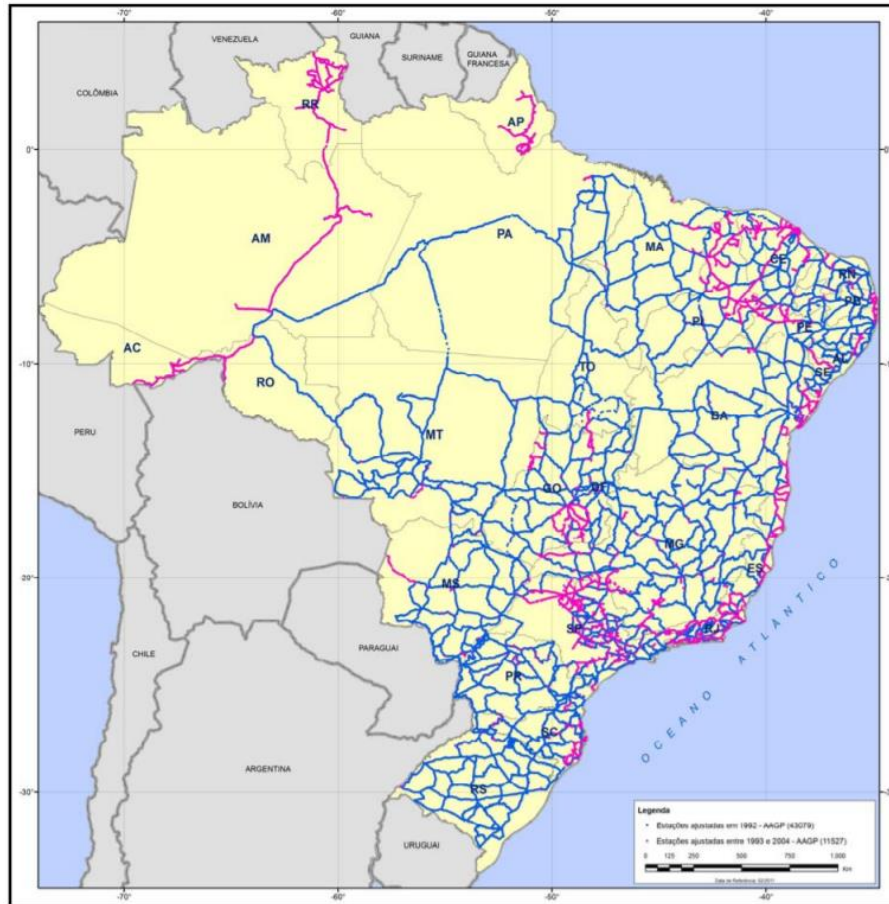
Introduction



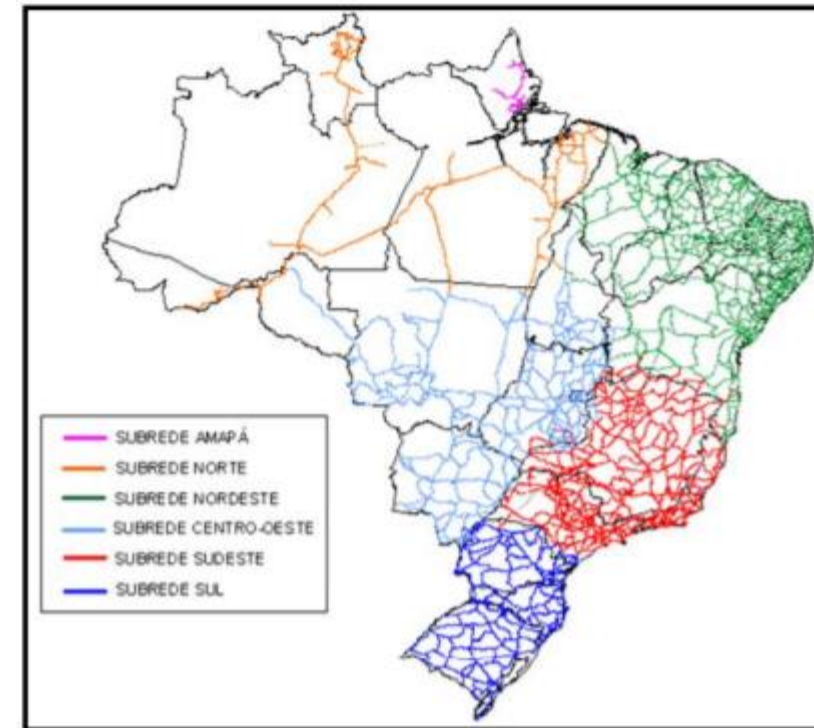
► BVRN historical evolution milestones



Previous BVRN adjustments (1948-1975)



Preliminary Global Altimetric Adjustment [AAGP] (1992-2004)

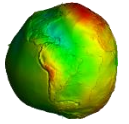


Global BVRN adjustment (2005-2011)

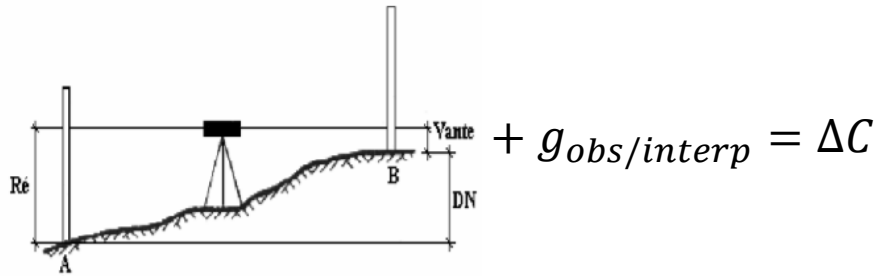
- GHOST software – NRCAN
- Helmert's blocking division – subnetworks
- Normal-orthometric correction

$$\delta H^{NOrt} \approx -2\alpha_1 H_m \Delta\varphi \text{sen}(2\varphi_m) [1 + (\alpha_1 - 2\alpha_2/\alpha_1) \cos(2\varphi_m)]$$

Introduction



- ▶ BVRN current adjustment (released in July 30th, 2018)
 - ▶ Adjustment in terms of geopotential numbers; altimetric information in form of normal heights



$$\Delta C_{AB} = C_B - C_A = -(W_A - W_B) \cong g_{obs/interp}^{AB} \cdot \Delta H_{obs}^{AB}$$

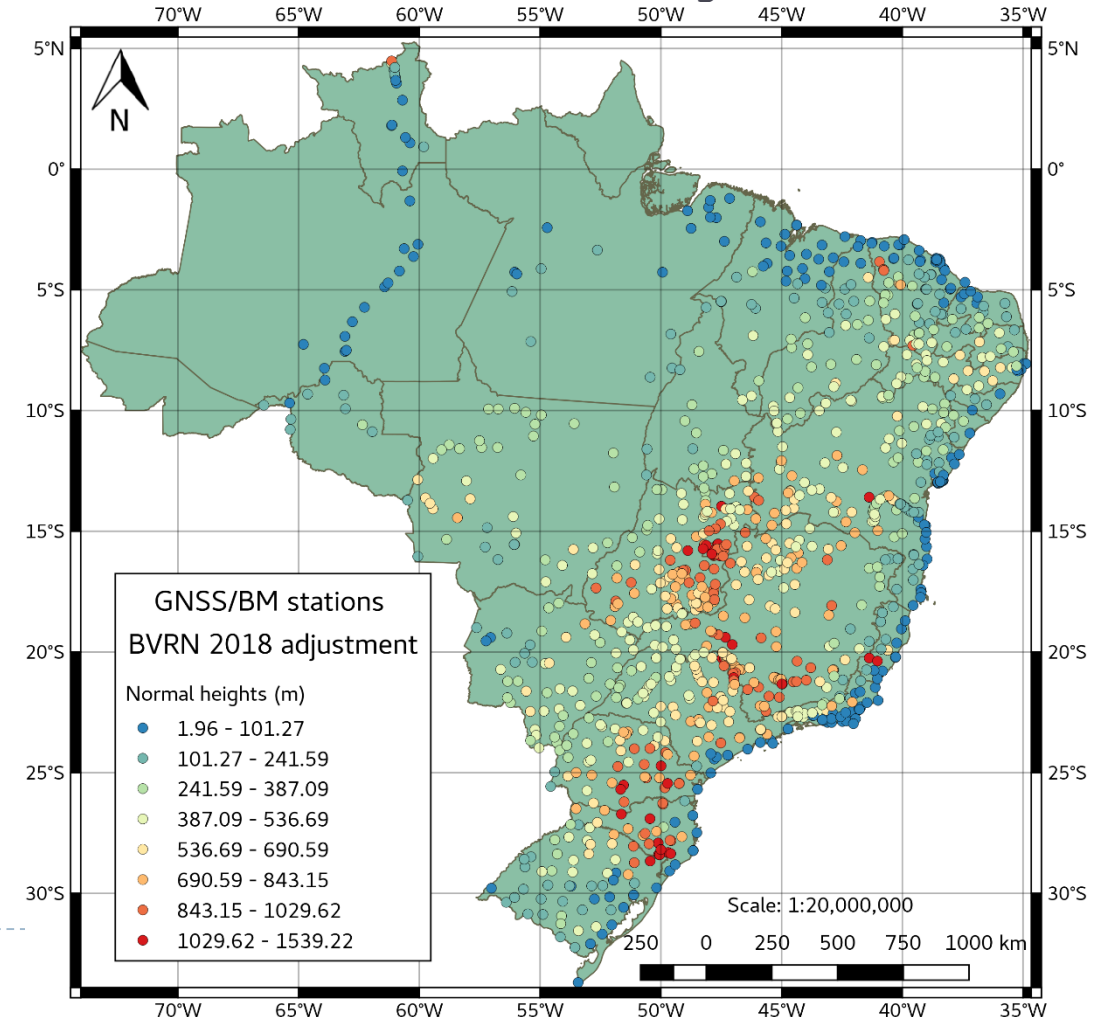
$$\Delta C \rightarrow X = N^{-1}U \rightarrow C_{adj}$$



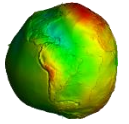
$$H^N = C_{adj} / \bar{\gamma}$$

$$\bar{\gamma} = \gamma_0 \left[1 - \frac{2}{a} (1 + f + m - 2f \sin^2 \varphi) H^N + 3 \left(\frac{H^N}{a} \right)^2 \right]$$

$$\gamma_0 = \frac{a \gamma_e \cos^2 \varphi + b \gamma_p \sin^2 \varphi}{\sqrt{a^2 \cos^2 \varphi + b^2 \sin^2 \varphi}} ; m = \frac{\omega^2 a^2 b}{GM}$$



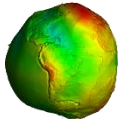
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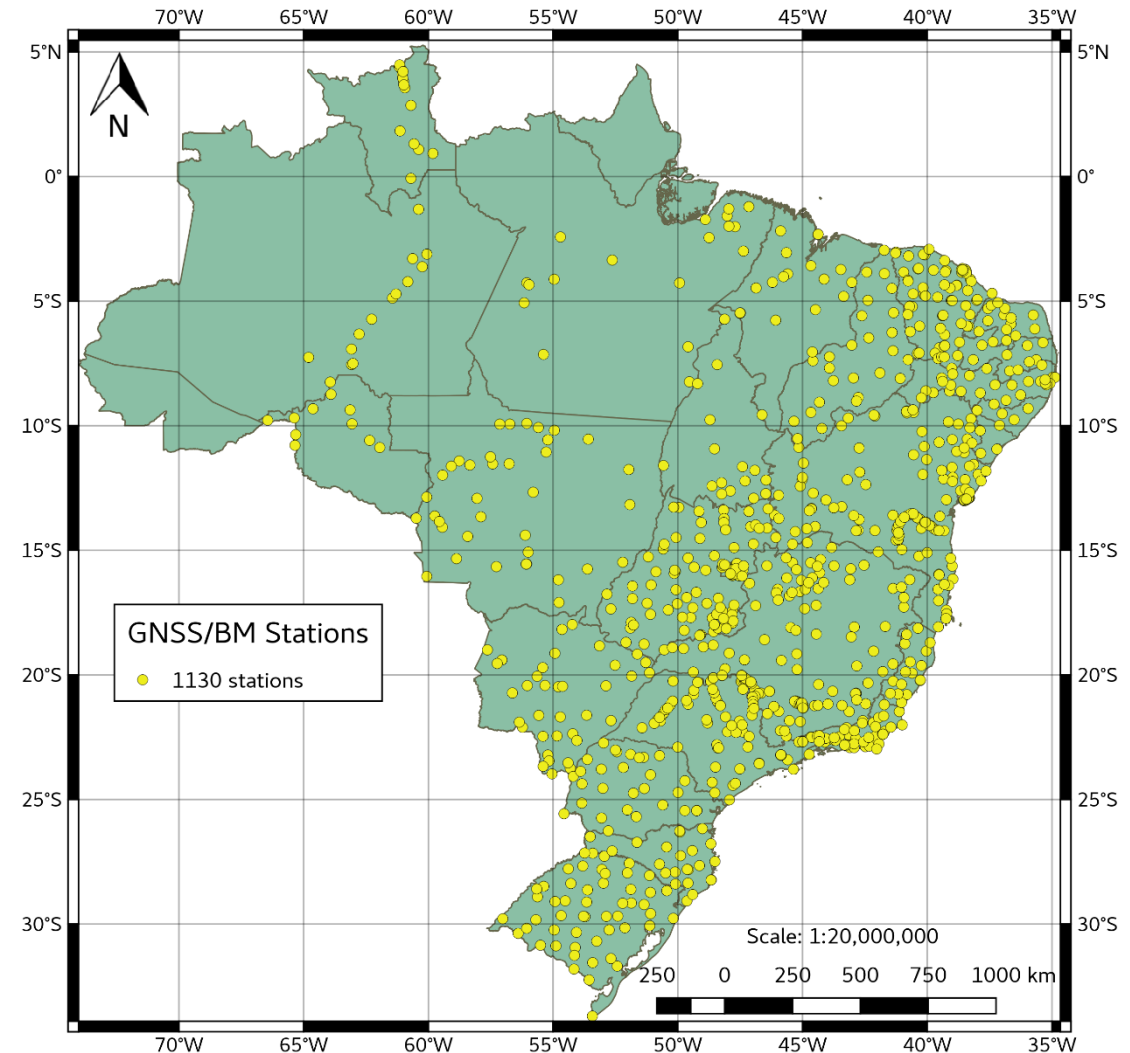
▶ Preliminary tests on BVRN normal heights main objectives

1. Perform comparisons of height anomalies provided from GNSS/BM information (h and H^N data available) with results calculated from GGMs with proven highlighted performance in previous studies/adjustment all along the study area;
2. Identify possible gains/losses with new representation of BVRN benchmarks in terms of normal heights;
3. Provide IBGE with relevant inconsistencies observed during preliminary tests, in order to enable further investigation.

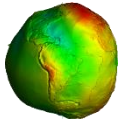
Study area



- ▶ Brazilian territory;
- ▶ 1162 stations of BVRN with connection with IBGE's SAT-GPS network – GNSS/BM stations
 - ▶ 1130 GNSS/BM stations - *stable* stations and linked to DVB-I
 - ▶ 32 under further investigation or linked to DVB-S
- ▶ Shapefile format [IBGE's BDG] – easier handling;
- ▶ Carry information of both ellipsoidal [h] and normal heights [H^N];
- ▶ Non-uniform distribution of stations acceptable for these preliminary tests.



GGMs employed



▶ Selection

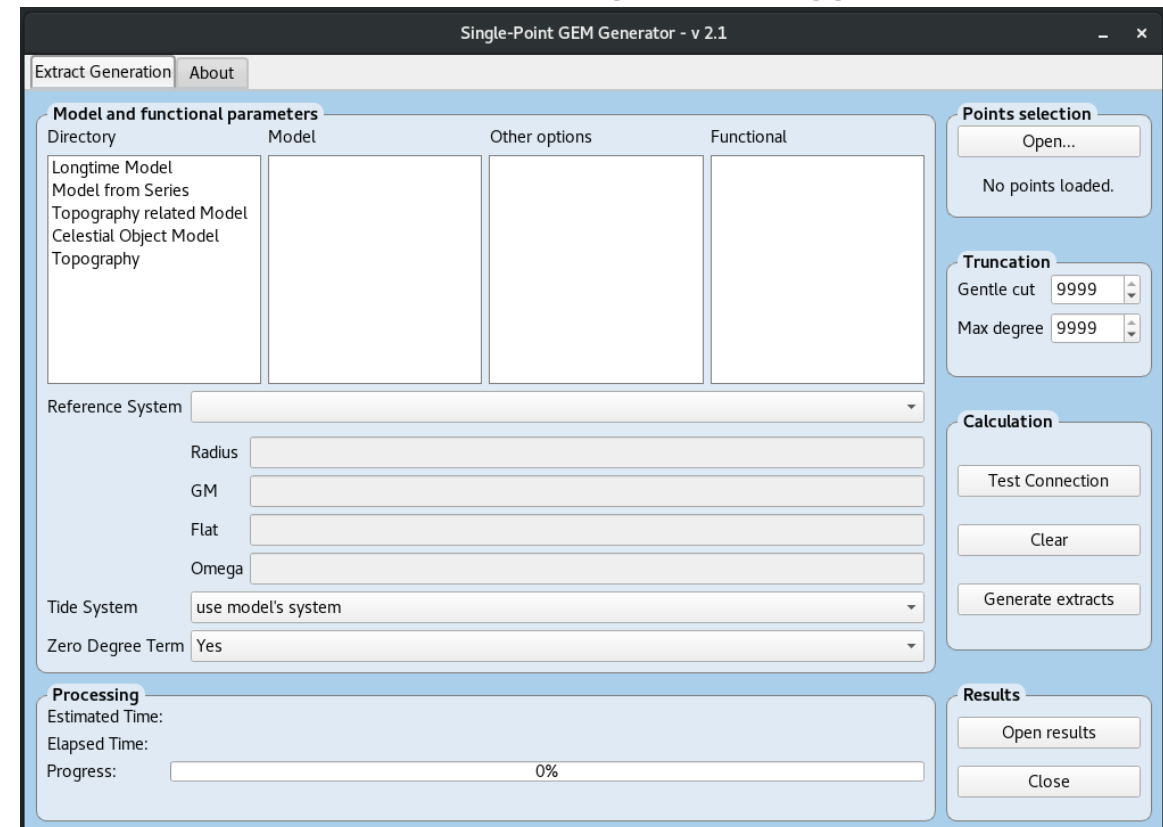
- ▶ Main combined GGMs since EGM2008;
- ▶ Proven to be highlights on metric geopotential functionals representation on the study area;
- ▶ Single geopotential functional: height anomaly.

GGM	Harmonic Degree		
EGM2008	2190	-	720
EIGEN-6C4	2190	-	720
SGG-UGM-I	-	2159	720
GOCO05C	-	-	720
XGM2016	-	-	719

▶ Acquisition

- ▶ SPGG v2.1 [pointwise approach]

(See: <https://euriconicacio.github.io/spgg/help/>)



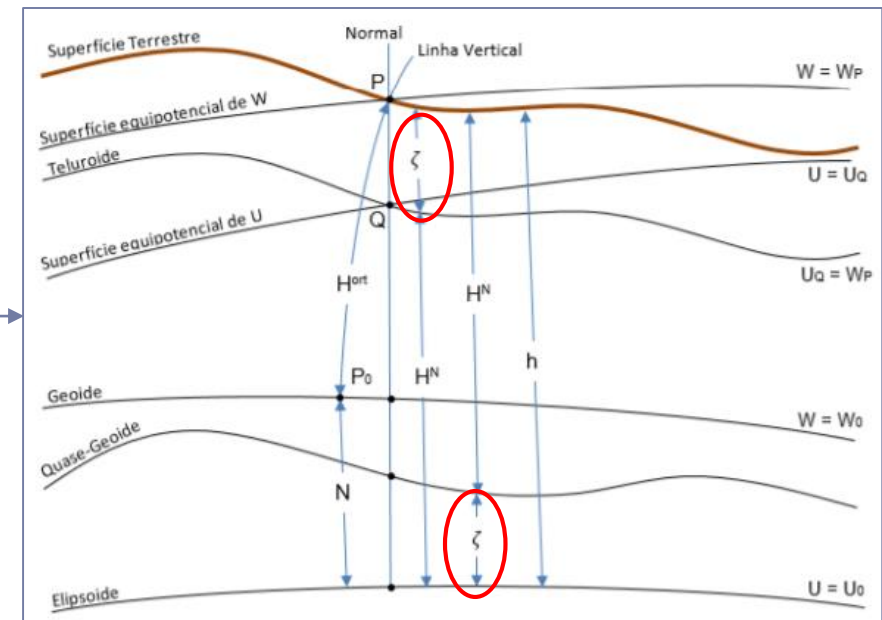
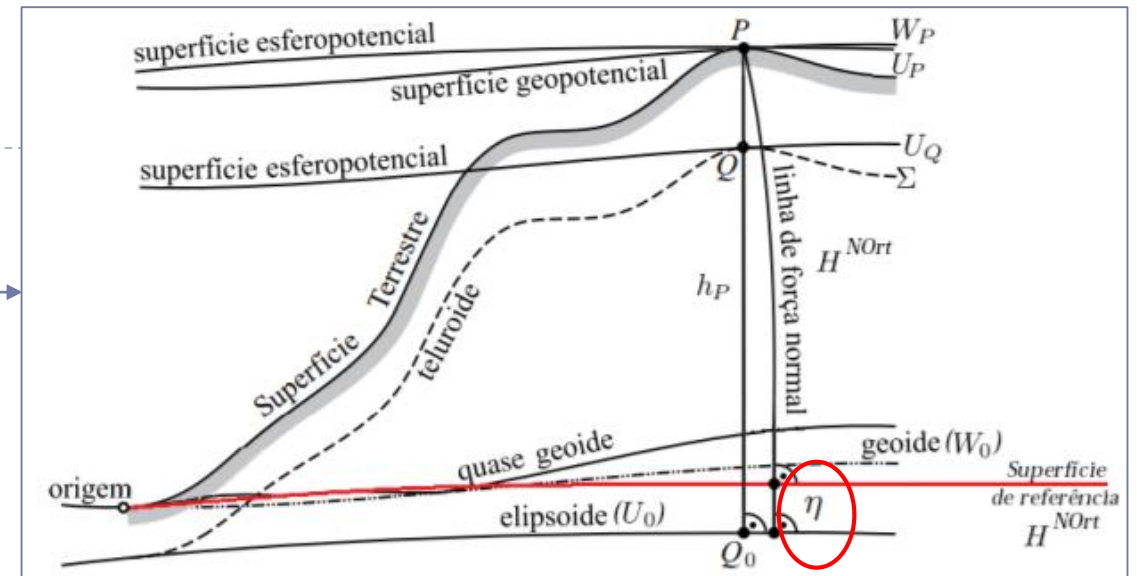
Height anomalies modelling

▶ Previous BVRN adjustment: normal-orthometric heights [H^{NOrt}]

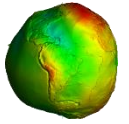
- ▶ Existence of normal-geoid height (η) concept: $h \cong H^{NOrt} + \eta$
- ▶ Normal-geoid heights (η) could be better modelled by height anomalies (ζ) or geoid heights (N), depending on the study área;

▶ Current BVRN adjustment: normal heights [H^N]

- ▶ Relation between ellipsoidal heights (h) and normal heights (H^N) given by height anomalies (ζ): $h \cong H^N + \zeta$



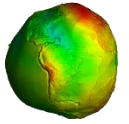
Height anomalies modelling – relative approach



- ▶ Featherstone (2001), Sánchez (2016), and Nicacio and Dalazoana (2018):
 - ▶ In order to mitigate additive errors inherent to the processing approach and to the obtaintion method of the GGMs, use of relative approach instead of the absolute one;
 - ▶ Absolute approach: $h \cong H^N + \zeta$
 - ▶ Relative approach: $\Delta h = \Delta H^N + \Delta \zeta \Rightarrow \zeta_P = \zeta_0 + h_P - h_0 - H_P^N + H_0^N$
 - ▶ Prior results confirm this is the most advisable alternative these days, specially under the aspect of vertical reference systems consecution.
- ▶ Permanent tide systems compatibilization [Ekman (1989), Mäkinen and Ihde (2006) and Tenzer et al. (2011)]:

$$h_{mean-tide} = h_{tide-free} - \left\{ (1 + k - h) \left[-0.198 \times \left(\frac{3}{2} \sin^2 \phi - \frac{1}{2} \right) \right] \right\}$$

Evaluation criteria

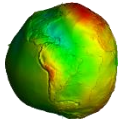


- ▶ Optimal configuration (OC) – model with minimum mean difference for the whole set of points

$$\left\{ \begin{array}{l} [\zeta_P]_{EGM2008} \\ [\zeta_P]_{EIGEN-6C4} \\ [\zeta_P]_{SGG-UGM-1} \\ [\zeta_P]_{GOCO05C} \\ [\zeta_P]_{XGM2016} \end{array} \right. \Rightarrow \min \theta_P = \left| |\zeta_P^{ref}| - |\zeta_P^{calc}| \right|$$

- ▶ Global evaluation (Brazil) and comparison with results for previous BVRN BMs representation [Nicacio et al. (2018) and Nicacio and Dalazoana (2017)].

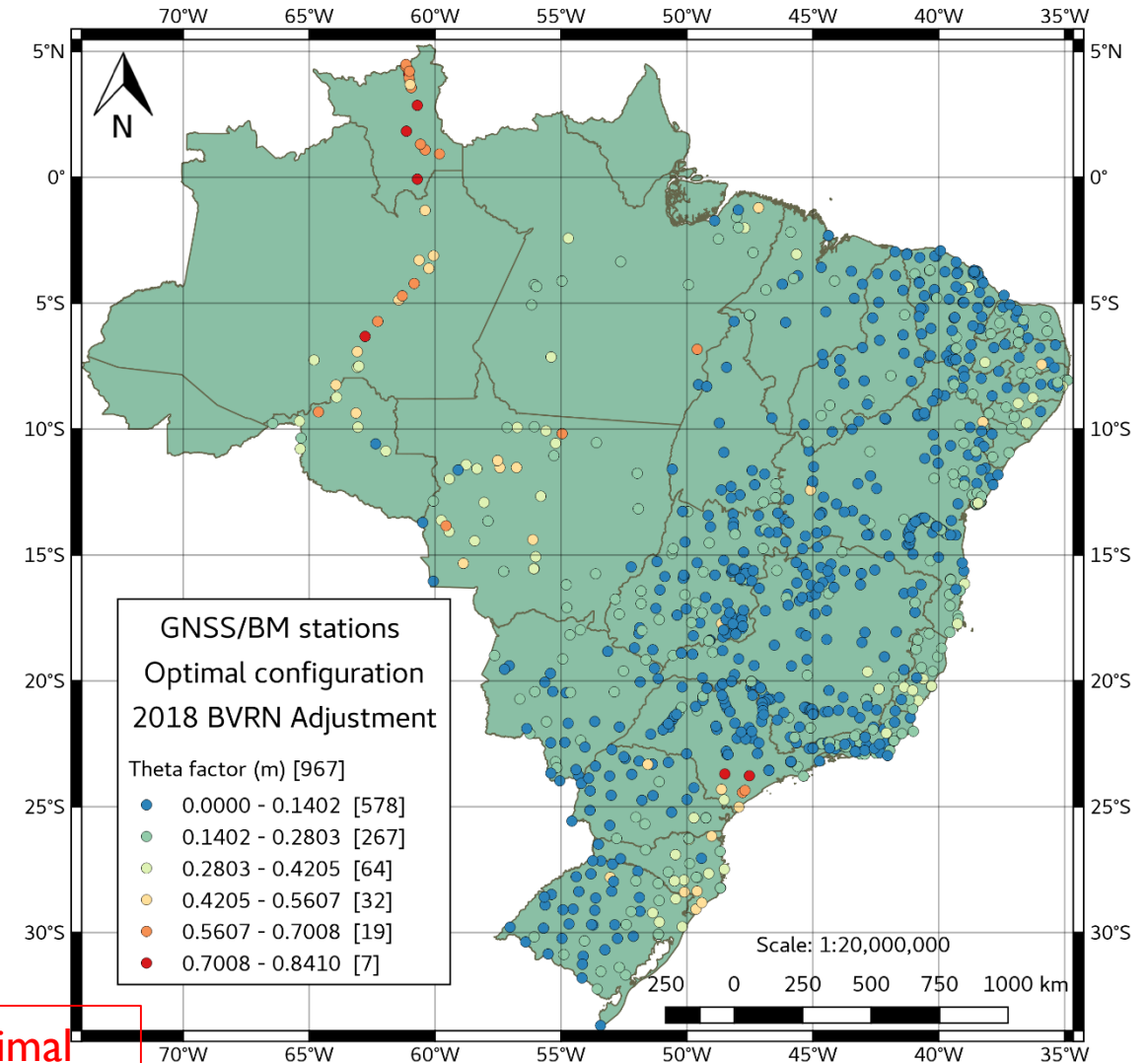
Results and discussions



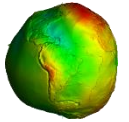
2018 Adjustment	GGM	DIF	DEGREE/ORDER		
			2190	2159	720/719
	EGM2008	MIN		0,0000	-
MEAN			0,1568	-	0,1618
MAX			1,2202	-	1,2252
RMS			0,1652	-	0,1668
EIGEN-6C4	MIN		0,0000	-	0,0000
	MEAN		0,1461	-	0,1565
	MAX		0,9097	-	1,0437
	RMS		0,1429	-	0,1546
SGG-UGM-1	MIN		-	0,0000	0,0000
	MEAN		-	0,1458	0,1531
	MAX		-	0,8938	0,9416
	RMS		-	0,1430	0,1480
GOCO05C	MIN		-	-	0,0000
	MEAN		-	-	0,1420
	MAX		-	-	0,8598
	RMS		-	-	0,1332
XGM2016	MIN		-	-	0,0000
	MEAN		-	-	0,1386
	MAX		-	-	0,8410
	RMS		-	-	0,1332

Differences statistics, in meters, between GNSS/BM solutions and GGM height anomalies modelling for current BVRN adjustment.

Optimal configuration



Results and discussions

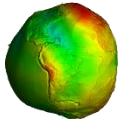


2011 Adjustment	GGM	DIF	DEGREE/ORDER AND FUNCTIONAL			
			2190		720	
			Geoid	Height Anom	Geoid	Height Anom
EGM2008	MIN	0,0000	0,0000	0,0000	0,0000	
	MEAN	0,1741	0,1712	0,1807	0,1773	
	MAX	2,9766	2,9651	2,9292	2,9107	
	RMS	0,2399	0,2354	0,2385	0,2337	
EIGEN-6C4	MIN	0,0000	0,0000	0,0000	0,0000	
	MEAN	0,1548	0,1521	0,1631	0,1612	
	MAX	1,1824	1,1463	1,1595	1,1208	
	RMS	0,1637	0,1613	0,1665	0,1632	
GOCO05C	MIN	-	-	0,0000	0,0000	
	MEAN	-	-	0,1528	0,1489	
	MAX	-	-	1,1345	1,1166	
	RMS	-	-	0,1554	0,1504	
XGM2016	MIN	-	-	0,0000	0,0000	
	MEAN	-	-	0,1496	0,1461	
	MAX	-	-	0,9738	0,9596	
	RMS	-	-	0,1518	0,1480	

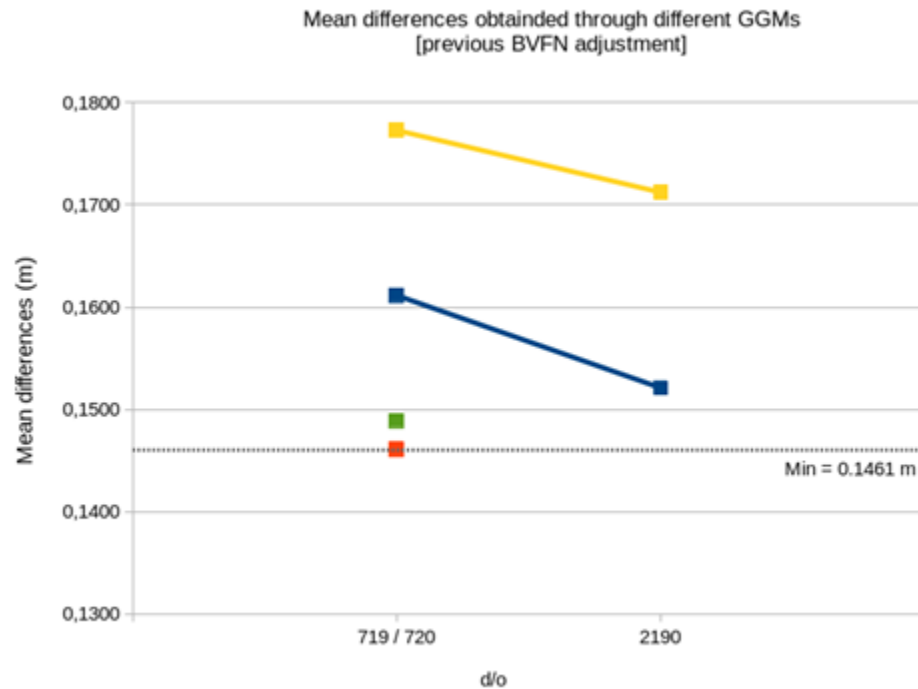
2018 Adjustment	GGM	DIF	DEGREE/ORDER		
			2190	2159	720/719
EGM2008	MIN	0,0000	-	0,0000	
	MEAN	0,1568	-	0,1618	
	MAX	1,2202	-	1,2252	
	RMS	0,1652	-	0,1668	
EIGEN-6C4	MIN	0,0000	-	0,0000	
	MEAN	0,1461	-	0,1565	
	MAX	0,9097	-	1,0437	
	RMS	0,1429	-	0,1546	
SGG-UGM-1	MIN	-	0,0000	0,0000	
	MEAN	-	0,1458	0,1531	
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	RMS	-	0,1430	0,1480	
GOCO05C	MIN	-	-	0,0000	
	MEAN	-	-	0,1420	
	MAX	-	-	0,8598	
	RMS	-	-	0,1332	
XGM2016	MIN	-	-	0,0000	
	MEAN	-	-	0,1386	
	MAX	-	-	0,8410	
	RMS	-	-	0,1332	

Optimal configuration

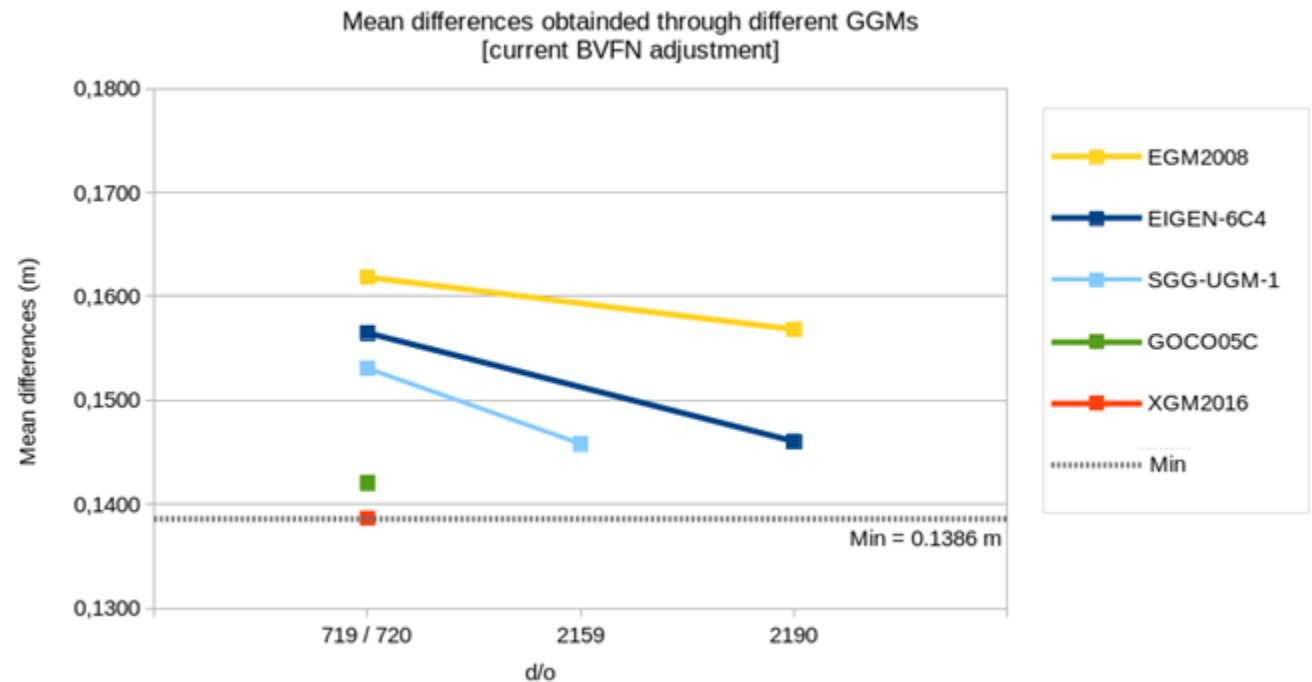
Results and discussions



Previous BVRN adjustment

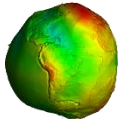


Current BVRN adjustment



- ▶ To sum up, results obtained with the GGMs tested presented significant gains in accuracy from previous to current BVRN adjustments.
- ▶ Optimal configuration kept (GGM XGM2016, height anomaly functional, d/o 719), with a ~ 1 cm gain in representation accuracy.

Conclusions and outlook

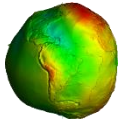


- ▶ Usage of the relative approach for handling GGMs is recommended;
- ▶ Relevant increase in the accuracy of altimetric representation with the adoption of normal heights, mainly when comparing mean discrepancies obtained from optimal configurations in each benchmark, for each height representation – both normal-orthometric and normal heights;
- ▶ Despite some point-wise and local inconsistencies, which are already under further investigation, the mean positive results are justified by a closer alignment to physical meaning when using normal heights;
- ▶ Furthermore, it must be emphasized the efforts made by IBGE in order to provide large scale products for the community with outstanding quality, clearly aiming at an advance towards a national alignment with the state-of-art, definitions and recommendations of the International Association of Geodesy (IAG);
- ▶ Validity for GNSS/levelling tests on Brazilian territory is still remarkable;
- ▶ Results limited to input information accuracy [h and H^N].

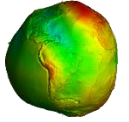
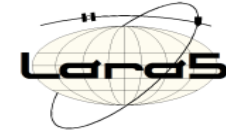
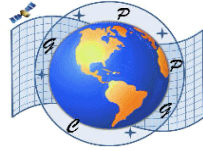
References



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- ▶ Local organizing Committee, SIRGAS 2018 Symposium.



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Cap QEM/Cart MSc Eurico Nicacio [euriconicaciojr@gmail.com]

Prof.^a Dr.^a Regiane Dalazoana [regiane@ufpr.br]

Prof. Dr. Silvio de Freitas [sfreitas@ufpr.br]

